

# Accounting for Density-Dependent Predation in the Survival of Juvenile Salmon and Steelhead During Their Seaward Migration

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# Motivation

- Substantial smolt mortality due to avian predators (Roby et al. 2003, Evans et al. 2012, Hostetter et al. 2015)
- and fish predators (Ward et al. 1995, Beamsderfer et al. 1996)
- There is need to provide more accurate survival estimates and model-based predictions

# Predator swamping

- Accumulation of large numbers of prey individuals in synchrony – saturates limited number of predators
- At high prey population size, each individual has higher probability of escaping predation



# Type II functional response

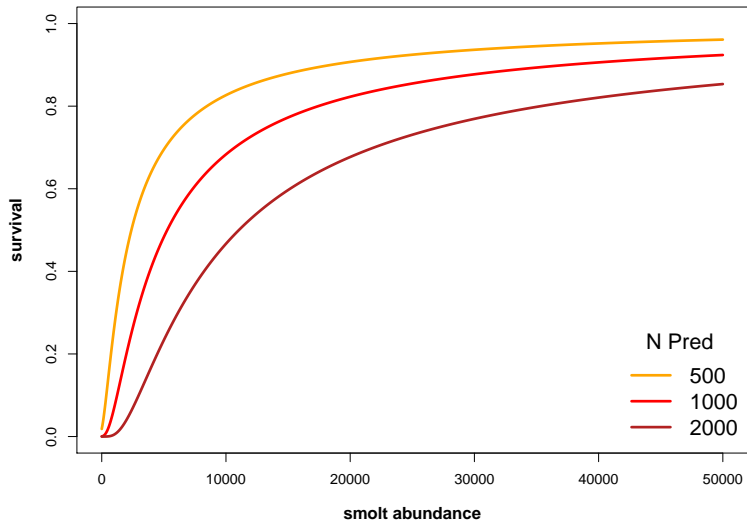
- Type II functional response

$$\frac{dN}{dt} = \frac{\alpha PN}{N + \gamma}$$

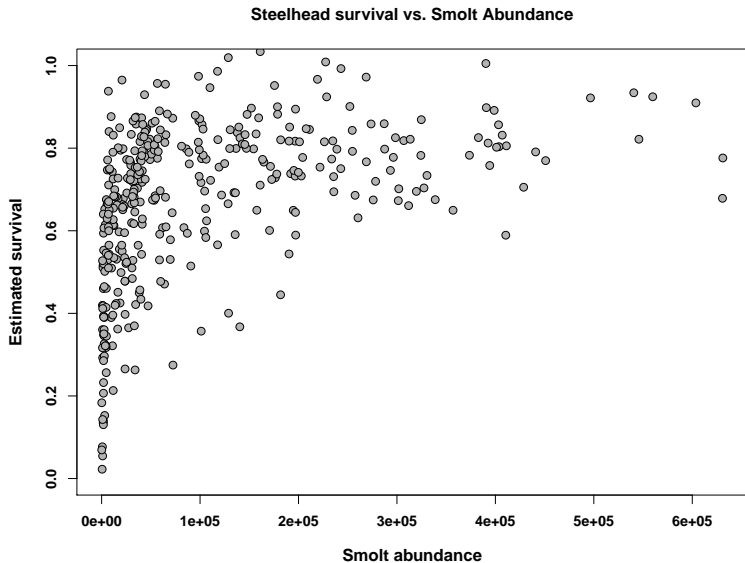
- An approximate solution gives

$$S_t = \exp \left\{ -\frac{\alpha P}{N_0 + \gamma} t \right\}$$

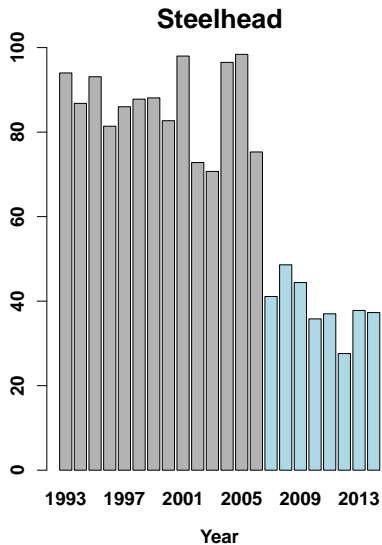
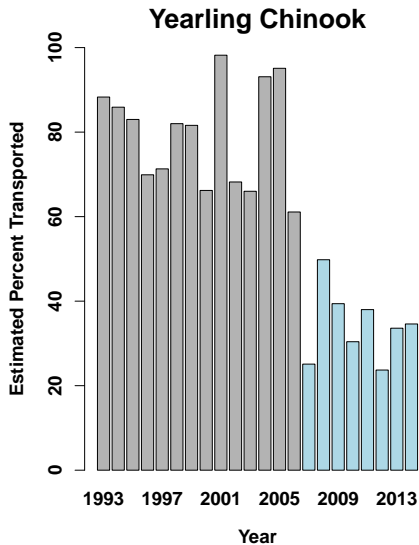
# Type II functional response



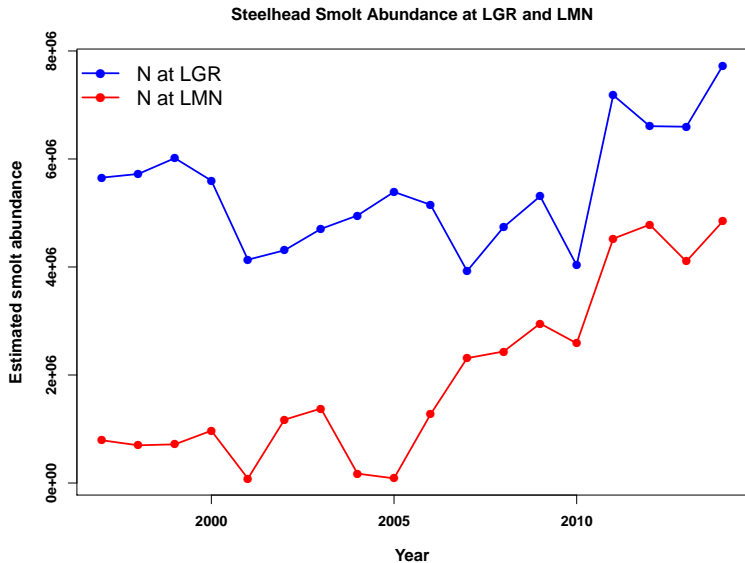
# Smolt survival data – Type II?



# Percent population transported



# Effect of transportation downstream

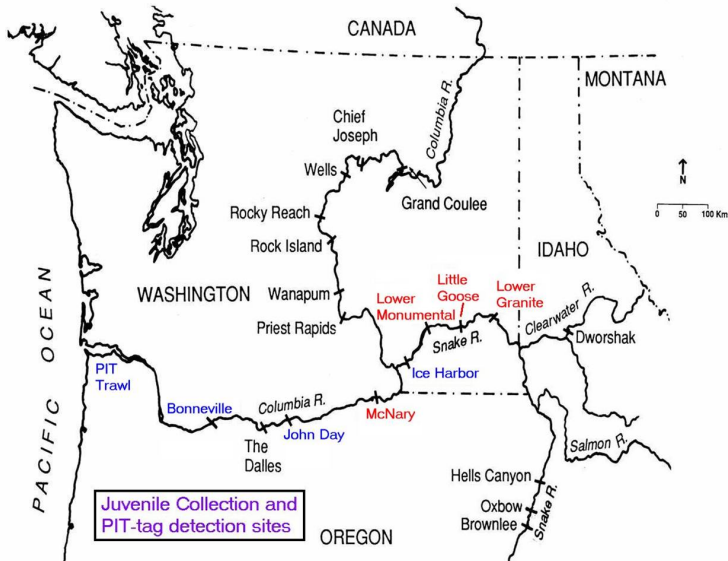




# Data Example: steelhead survival

- **Data:**
  - CJS survival estimates and SE's and travel time estimates for weekly release groups of PIT-tagged Snake River steelhead (hatchery and wild)
  - Lower Monumental to McNary (1998-2014) and Ice Harbor to McNary (2005-2014)
  - Population size estimates of steelhead in Ice Harbor and McNary pools
  - Population size estimates for Caspian terns on Crescent Island
  - Exposure indices for water velocity, temperature, and spill

# Study area



- Dam and reservoir mortality rates common to all models:

$$\lambda_r = \exp \{ \beta_0 + \beta_1 I_{\text{wild}} + \beta_2 \text{velocity} + \beta_3 \text{tempc} \}$$

$$\lambda_d = \exp \{ \omega_{0,M} + \omega_{1,M} \text{pspill}_M + (\omega_{0,I} + \omega_{1,I} \text{pspill}_I) I_{\text{mn}} \}$$

# Survival models

- ① Model 1: no predation, no smolt density

$$\mu = \exp\{-\lambda_d\} \exp\{-\lambda_r t\}$$

- ② Model 2: predation, no smolt density

$$\mu = \exp\{-\lambda_d\} \exp\{-(\lambda_r + \alpha P) t\}$$

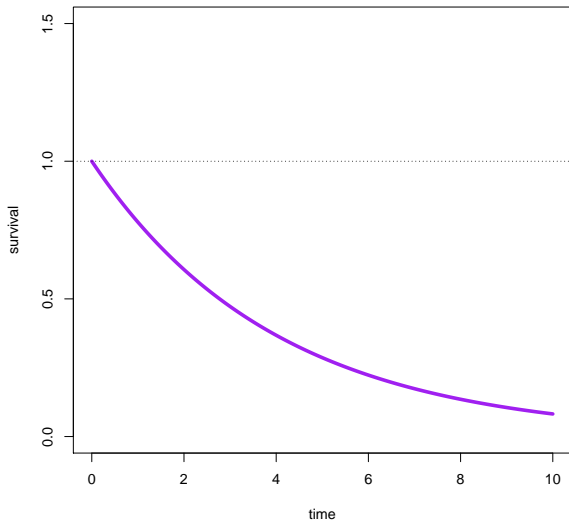
- ③ Model 3: predation and smolt density

$$\mu = \exp\{-\lambda_d\} \exp\left\{-\left(\lambda_r + \frac{\alpha P}{N + \gamma}\right) t\right\}$$

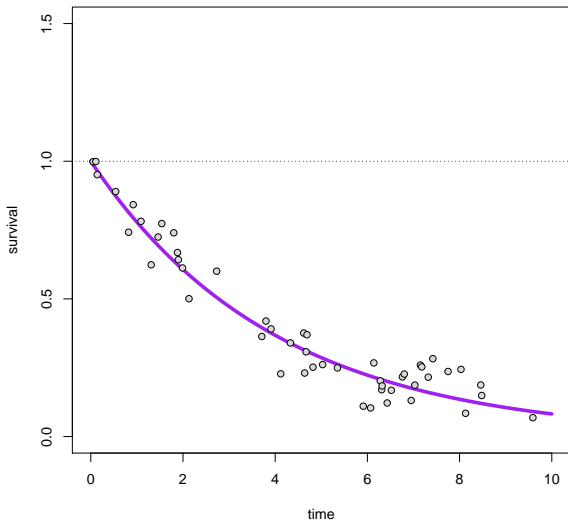
# CJS survival estimates as data

- Let  $y_i$  be a Cormack-Jolly-Seber (CJS) survival estimate for cohort  $i$  from a mark-recapture experiment,
- and  $\phi_i$  be unobserved true survival for cohort  $i$
- Problems:
  - CJS estimates can be  $> 1.0$
  - True survival is a probability between 0 and 1

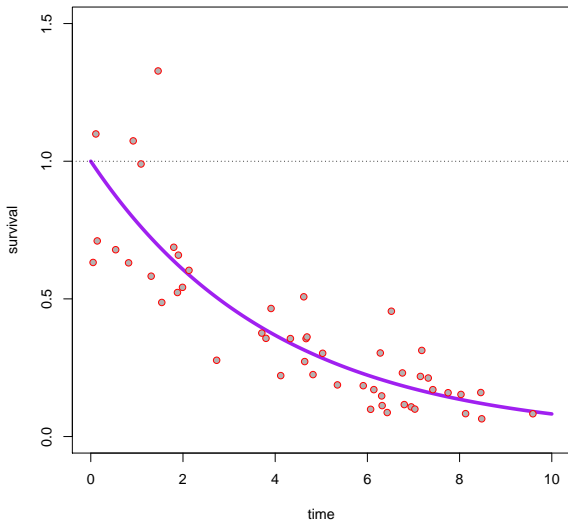
# Survival process



# Survival process and realized survival



# Survival process and estimated survival





# Accounting for uncertainty

- True unobserved survival for cohort  $i$

$$\phi_i \sim \text{Beta}(\mu_i, \tau)$$

where  $\mu_i = e^{-\lambda_i t_i}$

- Observed survival given true survival

$$y_i | \phi_i \sim \text{LogNormal}(\eta_i, \sigma_i^2),$$

where  $\eta_i$  and  $\sigma_i^2$  are the true unknown mean and sampling variance on the log scale

# Accounting for uncertainty

The  $\eta_i$  and  $\sigma_i^2$  are both functions of the coefficient of variation,  $\nu_i$ , where

$$\nu_i^2 = \frac{\text{Var}[y_i|\phi_i]}{\phi_i^2} \approx \frac{\hat{\text{Var}}[y_i|\phi_i]}{y_i^2}$$

That is,

$$\eta_i = \ln \left( \frac{\phi_i}{\sqrt{1 + \nu_i^2}} \right)$$

and

$$\sigma_i^2 = \ln(1 + \nu_i^2)$$

- Integrate over the unknown survival values (random effects) for each cohort

$$\begin{aligned} p(y_i | \boldsymbol{\theta}) &= \int_0^1 p(y_i | \phi_i, \boldsymbol{\theta}) p(\phi_i | \boldsymbol{\theta}) d\phi_i \\ &= \int_0^1 \text{LogNormal}(y_i | \phi_i, \boldsymbol{\theta}) \text{Beta}(\phi_i | \boldsymbol{\theta}) d\phi_i \end{aligned}$$

- Full likelihood is then

$$L(\mathbf{y} | \boldsymbol{\theta}) = \prod_{i=1}^n p(y_i | \boldsymbol{\theta})$$

# Posterior distribution

- In a Bayesian setting,

$$p(\boldsymbol{\theta} | \mathbf{y}) \propto \prod_{i=1}^n \int_0^1 p(y_i | \phi_i, \boldsymbol{\theta}) p(\phi_i | \boldsymbol{\theta}) d\phi_i p(\boldsymbol{\theta})$$

- Can implicitly marginalize by drawing from joint posterior

$$p(\boldsymbol{\phi}, \boldsymbol{\theta} | \mathbf{y}) \propto p(\mathbf{y} | \boldsymbol{\phi}, \boldsymbol{\theta}) p(\boldsymbol{\phi} | \boldsymbol{\theta}) p(\boldsymbol{\theta})$$

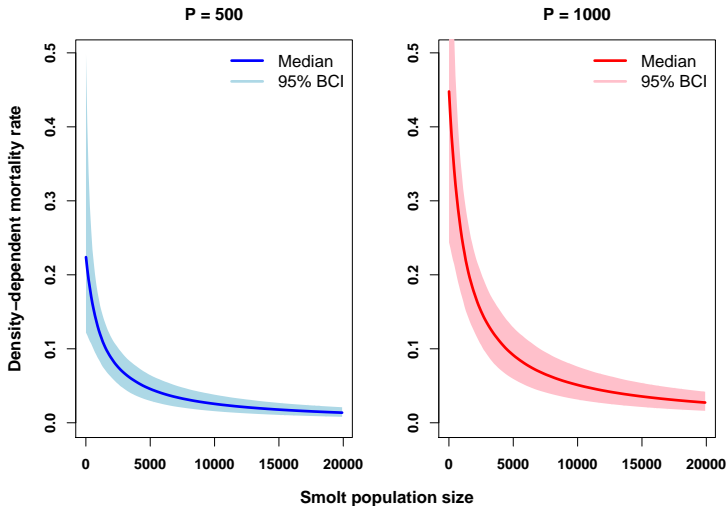
# Bayesian methods

- Non-informative priors on parameters
- Hamiltonian Monte Carlo
- Watanabe-AIC to compare for model selection

# Results

Model	Description	WAIC	$\Delta$ WAIC
1	No Pred, No Dens	-525.2	20.2
2	Pred, No Dens (Type I)	-524.5	21.1
3	Pred and Dens (Type II)	-545.6	0.0

# Posterior density-dependent mortality rates



# Conclusions

- Smolt density and predator density are important predictors of smolt survival
- Mortality rates increase with decreasing smolt densities
- Reduced transportation rates have resulted in more smolts remaining in river, which has likely contributed to higher in-river survival